

Mid-Term Exam, ECE-137B

Tuesday, May 3, 2016

Closed-Book Exam

There are 2 problems on this exam , and you have 75 minutes.

1) show all work. Full credit will not be given for correct answers if supporting work is not shown.

2) please write answers in provided blanks

3) Don't Panic !

4) 137a, 137b crib sheets, and 2 pages personal sheets permitted.

Use any, all reasonable approximations. After stating them. 5% accuracy is fine if the method is correct.

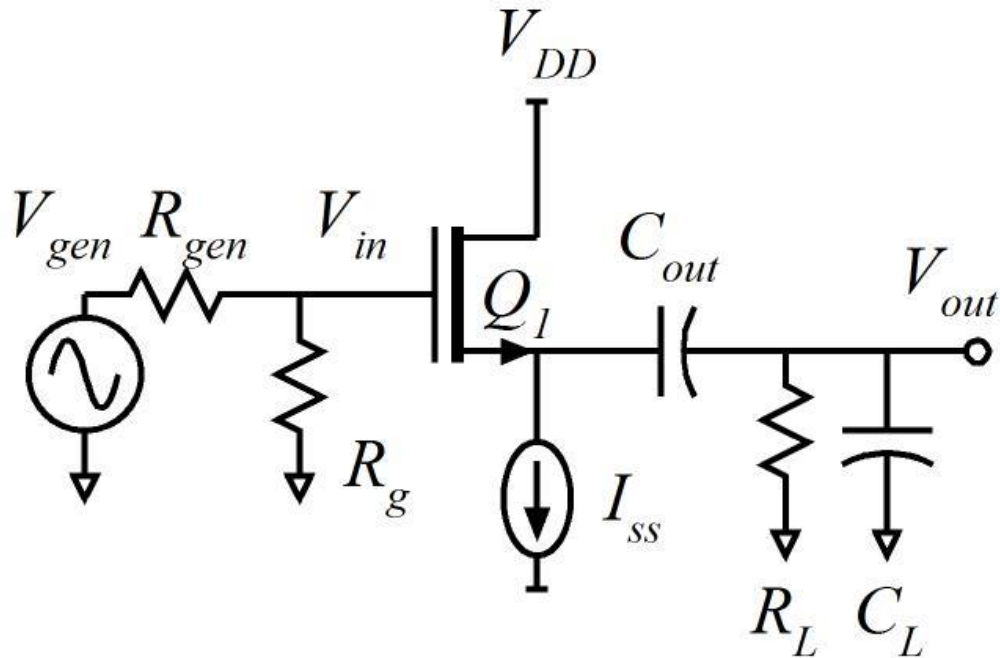
Do not turn over cover page until requested to do so.

Name: _____

Time function	LaPlace Transform
$\delta(t)$	1
$U(t)$	$1/s$
$e^{-\alpha t}U(t)$	$\frac{1}{s + \alpha}$
$e^{-\alpha t} \cos(\omega_d t)U(t)$	$\frac{s + \alpha}{(s + \alpha)^2 + \omega_d^2}$
$e^{-\alpha t} \sin(\omega_d t)U(t)$	$\frac{\omega_d}{(s + \alpha)^2 + \omega_d^2}$

Problem	Points Received	Points Possible
1a		2
1b		5
1c		4
1d		15
1e		7
1f		7
1g		5
2a		4
2b		6
2c		10
2d		5
3a		5
3b		10
3c		10
3d		5
total		100

Problem 1, 45 points



Q1 has 0.9 nm oxide thickness, $\epsilon_r=3.8$, 12 nm gate length, and a 0.2 V threshold.

Mobility is $400 \text{ cm}^2/(\text{V}\cdot\text{s})$, saturation drift velocity is $1\text{E}7 \text{ cm/s}$, $\lambda = 0 \text{ Volts}^{-1}$,

$C_{gs} = \epsilon_r \epsilon_{ox} L_g W_g / T_{ox} + (0.5\text{fF} / \mu\text{m}) \cdot W_g$ and $C_{gd} = (0.5\text{fF} / \mu\text{m}) \cdot W_g$.

calculated for you:

$\epsilon_r \epsilon_{ox} / T_{ox} = 3.74 \cdot 10^{-2} \text{ F/m}^2$, $(\mu c_{ox} W_g / 2L_g) = (6.23 \cdot 10^{-2} \text{ A/V}^2) \cdot (W_g / 1\mu\text{m})$

$(c_{ox} v_{sat} W_g) = (3.74 \cdot 10^{-3} \text{ A/V}^1) \cdot (W_g / 1\mu\text{m})$, $(v_{sat} L_g / \mu) = 30\text{mV}$.

VDD= +1V . ISS=4 mA.

You will pick the FET width W_g such that $V_{gs}=0.3\text{Volts}$ *

Rgen=100kOhm, Rg=1MOhm, RL=500 Ohms, CL=0fF.

Cout=10nF.

Part a, 2 points

Find the following:

$$W_g = \underline{\hspace{10em}}$$

Part b, 5 points

small-signal parameters

Find the following

$$C_{gs} = \underline{\hspace{2cm}} \quad C_{gd} = \underline{\hspace{2cm}}$$

$$g_m = \underline{\hspace{2cm}} \quad f_\tau = \underline{\hspace{2cm}}$$

Part c: 4 points

Mid Band Analysis:

Find the following:

$$R_{in, Amplifier} = \underline{\hspace{2cm}} \quad R_{L, eq} = \underline{\hspace{2cm}}$$

$$V_{out} / V_{in} = \underline{\hspace{2cm}} \quad V_{in} / V_{gen} = \underline{\hspace{2cm}}$$

Part d: 15 points

High-Frequency Analysis: Poles

Find the frequencies, in Hz, of the two poles limiting the high-frequency response of the amplifier. You can either use MOTC, or use the results derived in class (and written down on the class amplifier crib sheet). Hint: assume C_{out} is a short-circuit for this calculation

If the poles are real, give the 1 or 2 pole frequencies in Hz:

$$f_{p1, HF} = \underline{\hspace{2cm}} \quad f_{p2, HF} = \underline{\hspace{2cm}}.$$

If there are 2 poles, and they are complex, give $f_n = \omega_n / 2\pi$ and the damping factor ζ :

$$f_n = \omega_n / 2\pi = \underline{\hspace{2cm}}, \quad \zeta = \underline{\hspace{2cm}}$$

Part e: 7 points

High-Frequency Analysis: Zeros

Find the frequencies of any zeros (there may be zero, one or two present) in the transfer function. You can either use nodal analysis, or use the results derived in class (and written down on the class amplifier crib sheet).

$$f_{z1} = \text{_____}, f_{z2} = \text{_____}, \dots$$

Part f: 7 points

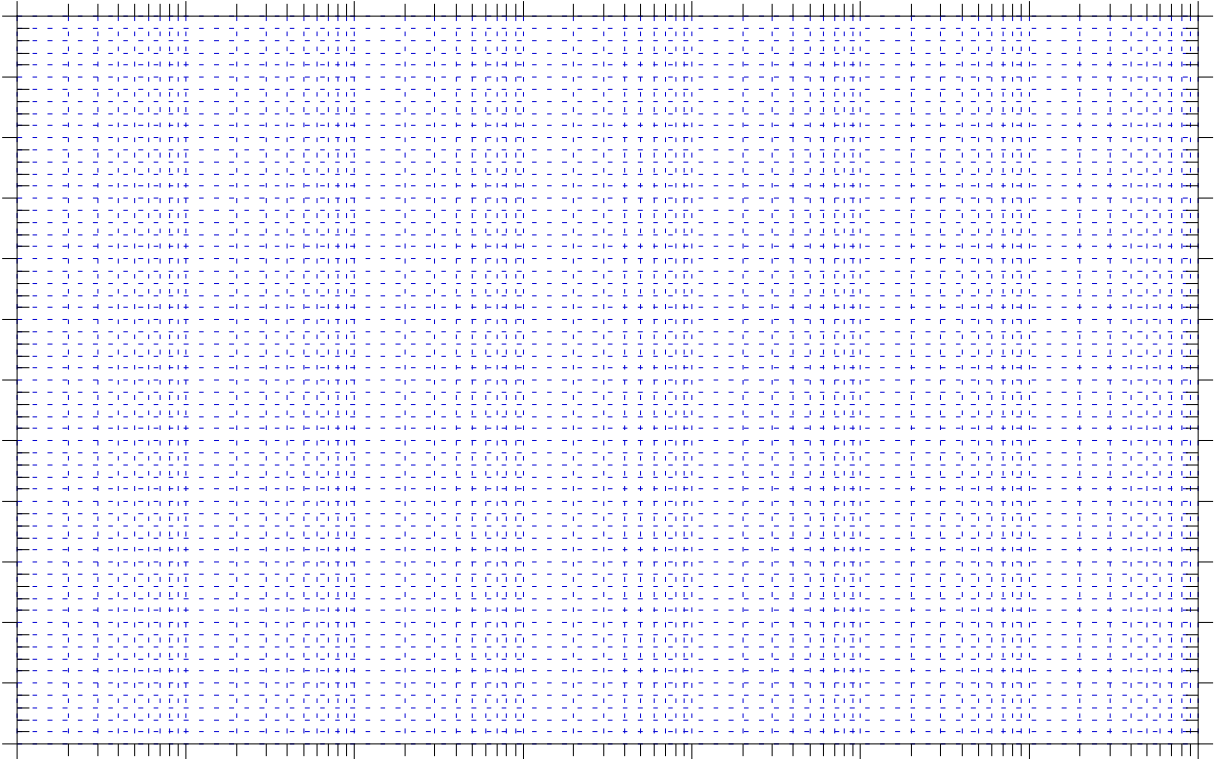
Low-Frequency Analysis:

Find the frequency in Hz, of the pole, due to C_{out} , limiting the low-frequency response of the amplifier. Use any method of analysis you choose.

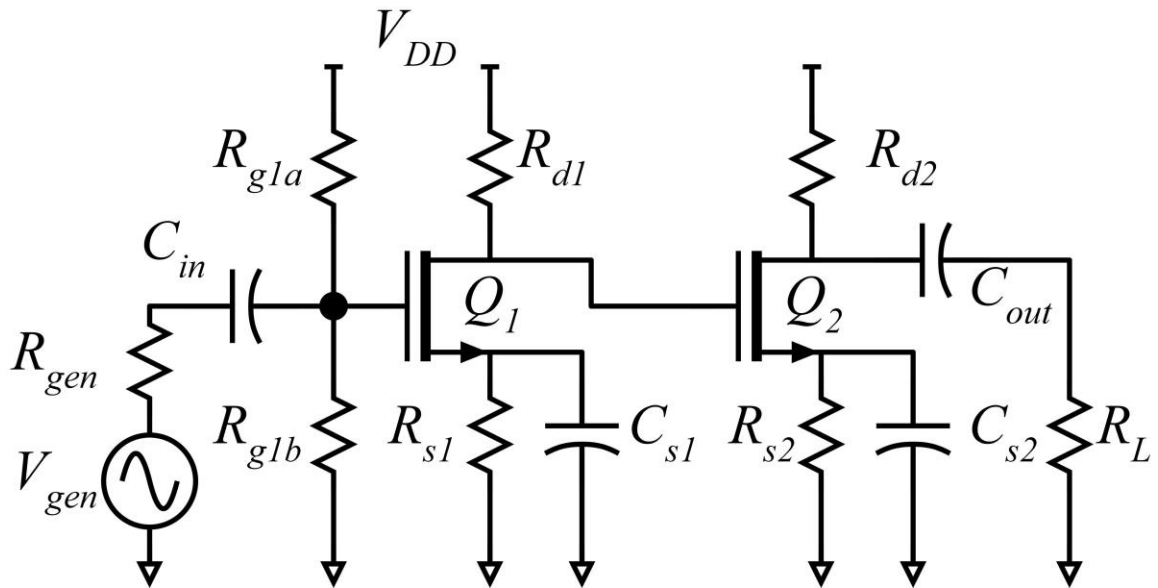
$$f_{p1,LF} = \underline{\hspace{10em}}$$

Part g: 5 points

Draw a clean asymptotic Bode Magnitude plot of V_{out}/V_{gen} as a function of frequency in Hz. Be sure to label and dimension the axes clearly, label pole and zero frequencies and gain slopes. Be sure to use the semi-log paper correctly



Problem 2, 25 points



In the amplifier above,
 $R_{gen}=100\text{k}\Omega$, $R_{g1a}=R_{g1b}=500\text{k}\Omega$,
 $R_{s1}=R_{s2}=100\ \Omega$. $V_{DD}=5\text{Volts}$
 $g_{m1}=5\ \text{mS}$, $g_{m2}=10\text{mS}$
 $R_{d1}=1\ \text{k}\Omega$, $R_{d2}=2\text{k}\Omega$, $R_L=10\text{k}\Omega$.
 C_{in} , C_{out} , C_{s1} , C_{s2} are all very large
 $C_{gs1}=0\text{fF}$, $C_{g1d}=5\text{fF}$, $C_{gs2}=20\ \text{fF}$, $C_{gd2}=0\text{fF}$
 $G_{ds1}=G_{ds2}=0\text{mS}$

Part a: 4 points

draw below a small-signal representation of the circuit, but with the transistors represented by transistor symbols, not small-signal hybrid-pi models

Part b, 6 points

Find the small-signal voltage gain of the two stages:

$$V_{out1}/V_{in1}=V_{d1}/V_{g1}=\underline{\hspace{2cm}}$$

$$V_{out}/V_{in2}=V_{d2}/V_{g2}=\underline{\hspace{2cm}}$$

Part c, 10 points

using the method of time constants, find a_1 and a_2 of the circuit transfer function:

$a_1 =$ _____

$a_2 =$ _____

Part d, 5 points

There may be either 1 or 2 poles of the transfer function.

If the poles are real, give the 1 or 2 pole frequencies in Hz:

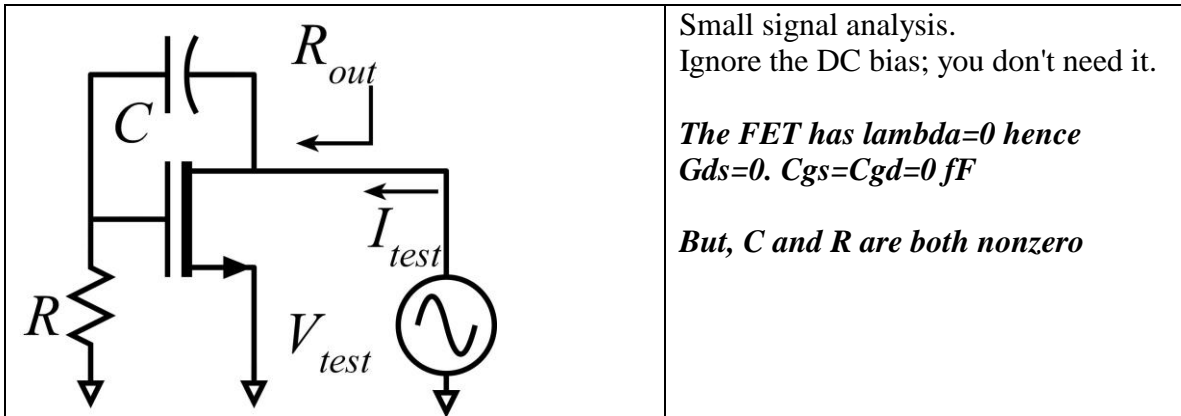
$$f_{p1} = \underline{\hspace{2cm}}, \quad f_{p2} = \underline{\hspace{2cm}}$$

If there are 2 poles, and they are complex, give $f_n = \omega_n / 2\pi$ and the damping factor ζ :

$$f_n = \omega_n / 2\pi = \underline{\hspace{2cm}}, \quad \zeta = \underline{\hspace{2cm}}$$

Problem 3, 30 points

Part a 5 points



Replacing the transistor with its high frequency small-signal model, draw a small-signal equivalent circuit diagram.

Part b, 10 points

USING NODAL ANALYSIS, compute $Z(s)=V_{\text{test}}(s)/I_{\text{test}}(s)$ in ratio-of-polynomials form:

$$Z(s) = Z_{\text{mid-band}} \times (s\tau)^m \times \frac{1 + b_1s + b_2s^2 + \dots}{1 + a_1s + a_2s^2 + \dots} = \underline{\hspace{10cm}}$$

here m , an integer, can be positive or negative or zero

Part c, 10 points

$$g_m = 1 \text{ mS}, R = 100 \text{ k}\Omega, C = 1 \text{ pF}$$

Find the frequencies of any zeros (there may be zero, one or two present) in $Z(s)$:

$$f_{z1} = \text{_____}, f_{z2} = \text{_____}, \dots$$

There may be either 1 or 2 poles in $Z(s)$.

If the poles are real, give the 1 or 2 pole frequencies in Hz:

$$f_{p1} = \text{_____}, f_{p2} = \text{_____}$$

If there are 2 poles, and they are complex, give $f_n = \omega_n / 2\pi$ and the damping factor ζ :

$$f_n = \omega_n / 2\pi = \text{_____}, \zeta = \text{_____}$$

Part d, 5 points

Can you describe the behavior of $Z(s)$ in terms of a simpler equivalent circuit ?