

## Mid-Term Exam, ECE-137B

Tuesday, May 3, 2016

### Closed-Book Exam

There are 2 problems on this exam , and you have 75 minutes.

**1) show all work. Full credit will not be given for correct answers if supporting work is not shown.**

2) please write answers in provided blanks

3) Don't Panic !

4) 137a, 137b crib sheets, and 2 pages personal sheets permitted.

Use any, all reasonable approximations. After stating them. 5% accuracy is fine if the method is correct.

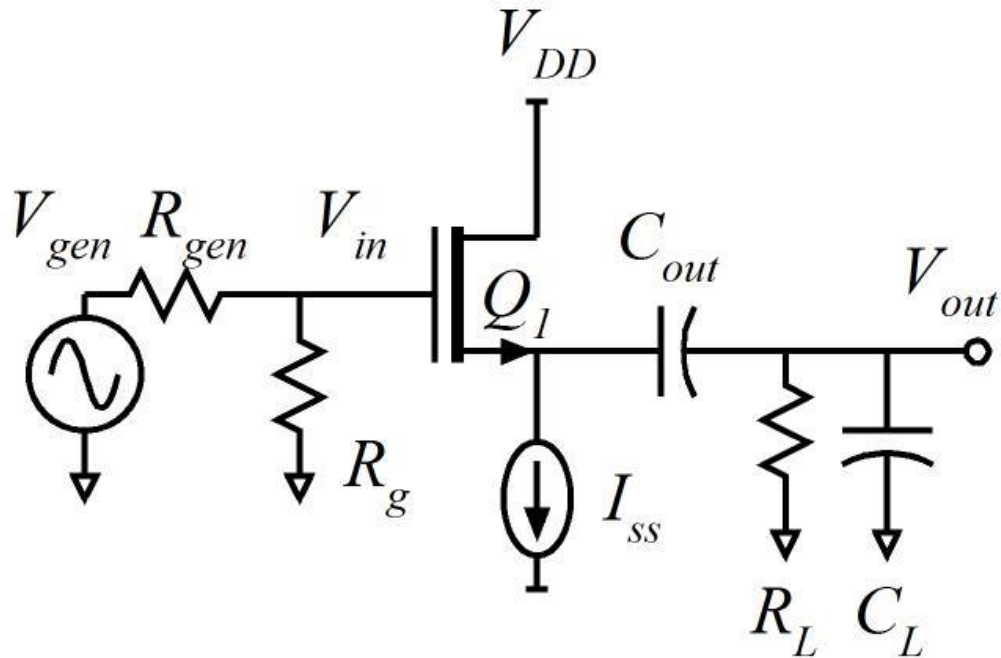
**Do not turn over cover page until requested to do so.**

Name: \_\_\_\_\_

Time function	LaPlace Transform
$\delta(t)$	1
$U(t)$	$1/s$
$e^{-\alpha t}U(t)$	$\frac{1}{s + \alpha}$
$e^{-\alpha t} \cos(\omega_d t)U(t)$	$\frac{s + \alpha}{(s + \alpha)^2 + \omega_d^2}$
$e^{-\alpha t} \sin(\omega_d t)U(t)$	$\frac{\omega_d}{(s + \alpha)^2 + \omega_d^2}$

Problem	Points Received	Points Possible
1a		2
1b		5
1c		4
1d		15
1e		7
1f		7
1g		5
2a		4
2b		6
2c		10
2d		5
3a		5
3b		10
3c		10
3d		5
total		100

**Problem 1, 45 points**



Q1 has 0.9 nm oxide thickness,  $\epsilon_r=3.8$ , 12 nm gate length, and a 0.2 V threshold.

Mobility is  $400 \text{ cm}^2/(\text{V}\cdot\text{s})$ , saturation drift velocity is  $1\text{E}7 \text{ cm/s}$ ,  $\lambda = 0 \text{ Volts}^{-1}$ ,

$C_{gs} = \epsilon_r \epsilon_{ox} L_g W_g / T_{ox} + (0.5\text{fF} / \mu\text{m}) \cdot W_g$  and  $C_{gd} = (0.5\text{fF} / \mu\text{m}) \cdot W_g$ .

calculated for you:

$\epsilon_r \epsilon_{ox} / T_{ox} = 3.74 \cdot 10^{-2} \text{ F/m}^2$ ,  $(\mu c_{ox} W_g / 2L_g) = (6.23 \cdot 10^{-2} \text{ A/V}^2) \cdot (W_g / 1\mu\text{m})$

$(c_{ox} v_{sat} W_g) = (3.74 \cdot 10^{-3} \text{ A/V}^1) \cdot (W_g / 1\mu\text{m})$ ,  $(v_{sat} L_g / \mu) = 30\text{mV}$ .

VDD= +1V . ISS=2 mA.

\*\*You will pick the FET width  $W_g$  such that  $V_{gs}=0.25\text{Volts}$ \*\*\*

Rgen=100kOhm, Rg=1MOhm, RL=500 Ohms, CL=0fF.

Cout=1nF.

Part a, 2 points

Find the following:

$$W_g = \underline{\hspace{10em}}$$

Part b, 5 points

*small-signal parameters*

Find the following

$$C_{gs} = \underline{\hspace{2cm}} \quad C_{gd} = \underline{\hspace{2cm}}$$

$$g_m = \underline{\hspace{2cm}} \quad f_\tau = \underline{\hspace{2cm}}$$

Part c: 4 points

*Mid Band Analysis:*

Find the following:

$$R_{in, Amplifier} = \underline{\hspace{2cm}} \quad R_{L, eq} = \underline{\hspace{2cm}}$$

$$V_{out} / V_{in} = \underline{\hspace{2cm}} \quad V_{in} / V_{gen} = \underline{\hspace{2cm}}$$

Part d: 15 points

*High-Frequency Analysis: Poles*

Find the frequencies, in Hz, of the two poles limiting the high-frequency response of the amplifier. You can either use MOTC, or use the results derived in class (and written down on the class amplifier crib sheet). Hint: assume  $C_{out}$  is a short-circuit for this calculation

If the poles are real, give the 1 or 2 pole frequencies in Hz:

$$f_{p1, HF} = \underline{\hspace{2cm}} \quad f_{p2, HF} = \underline{\hspace{2cm}}.$$

If there are 2 poles, and they are complex, give  $f_n = \omega_n / 2\pi$  and the damping factor  $\zeta$  :

$$f_n = \omega_n / 2\pi = \underline{\hspace{2cm}}, \quad \zeta = \underline{\hspace{2cm}}$$



Part e: 7 points

*High-Frequency Analysis: Zeros*

Find the frequencies of any zeros (there may be zero, one or two present ) in the transfer function. You can either use nodal analysis, or use the results derived in class (and written down on the class amplifier crib sheet).

$$f_{z1} = \text{_____}, f_{z2} = \text{_____}, \dots$$



Part f: 7 points

*Low-Frequency Analysis:*

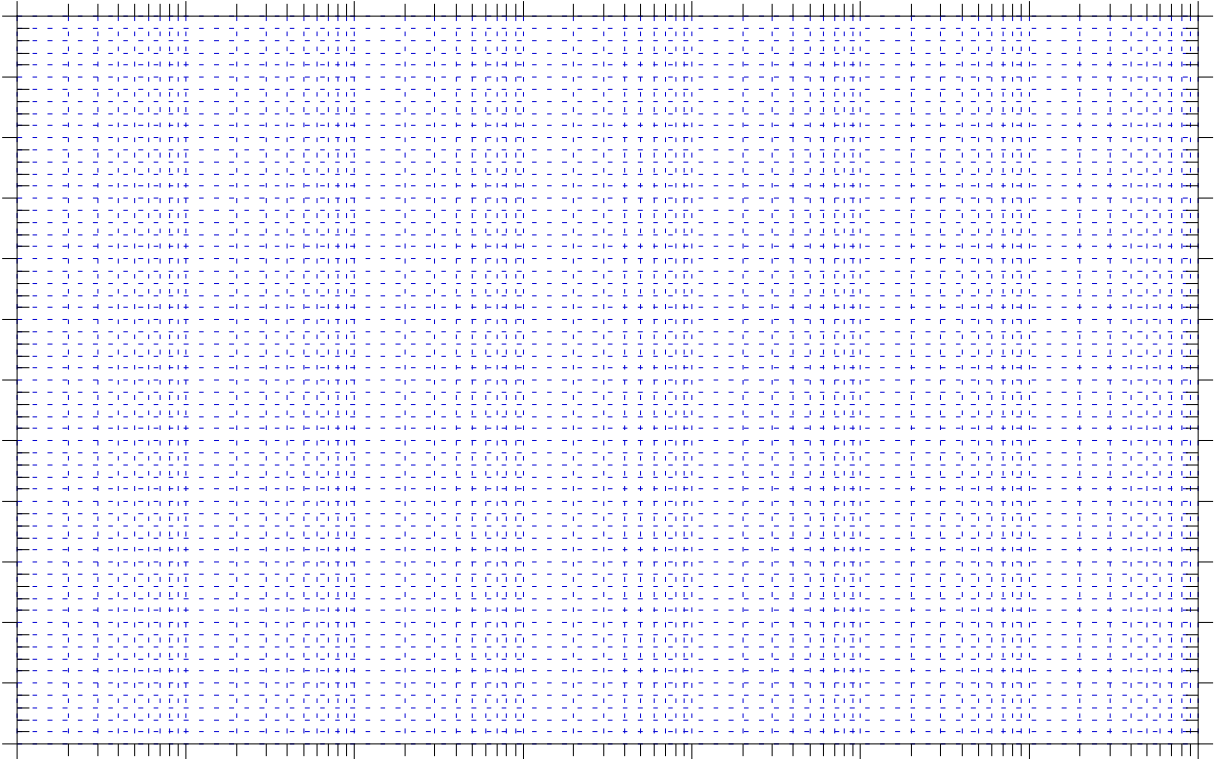
Find the frequency in Hz, of the pole, due to  $C_{out}$ , limiting the low-frequency response of the amplifier. Use any method of analysis you choose.

$$f_{p1,LF} = \underline{\hspace{10em}}$$

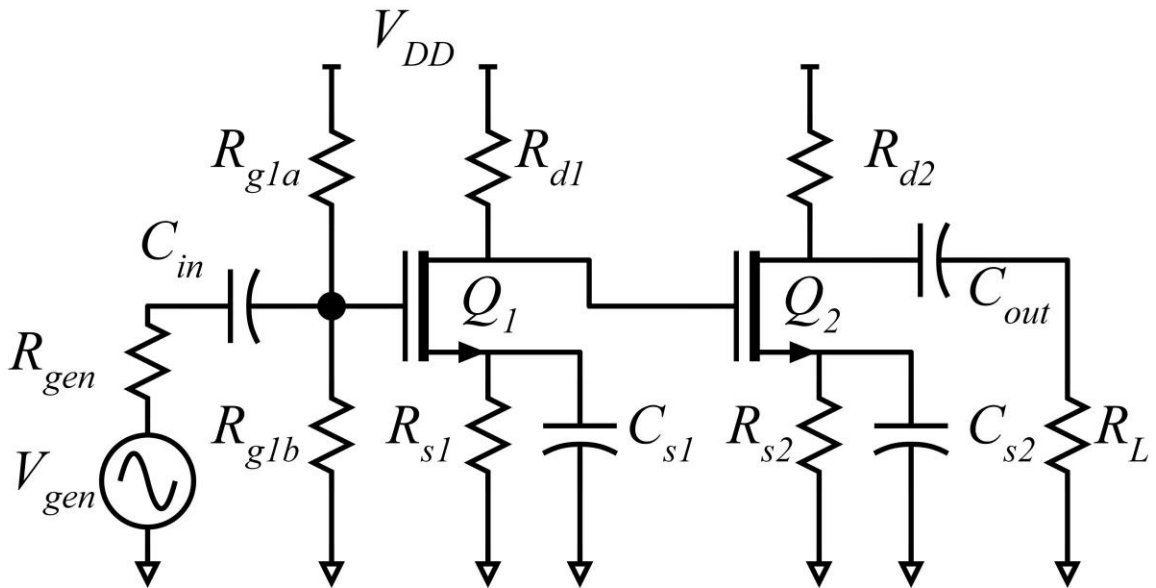


Part g: 5 points

Draw a clean asymptotic Bode Magnitude plot of  $V_{out}/V_{gen}$  as a function of frequency in Hz. Be sure to label and dimension the axes clearly, label pole and zero frequencies and gain slopes. Be sure to use the semi-log paper correctly



**Problem 2, 25 points**



In the amplifier above,  
 $R_{gen}=100\text{k}\Omega$ ,  $R_{g1a}=R_{g1b}=500\text{k}\Omega$ ,  
 $R_{s1}=R_{s2}=100\ \Omega$ .  $V_{DD}=5\text{Volts}$   
 $g_{m1}=5\ \text{mS}$ ,  $g_{m2}=10\text{mS}$   
 $R_{d1}=1\ \text{k}\Omega$ ,  $R_{d2}=2\text{k}\Omega$ ,  $R_L=10\text{k}\Omega$ .  
 $C_{in}$ ,  $C_{out}$ ,  $C_{s1}$ ,  $C_{s2}$  are all very large  
 $C_{gs1}=0\text{fF}$ ,  $C_{gd1}=5\text{fF}$ ,  $C_{gs2}=0\ \text{fF}$ ,  $C_{gd2}=10\text{fF}$   
 $G_{ds1}=G_{ds2}=0\text{mS}$

**Part a: 4 points**

draw below a small-signal representation of the circuit, but with the transistors represented by transistor symbols, not small-signal hybrid-pi models

Part b, 6 points

Find the small-signal voltage gain of the two stages:

$$V_{out1}/V_{in1} = V_{d1}/V_{g1} = \underline{\hspace{2cm}}$$

$$V_{out}/V_{in2} = V_{d2}/V_{g2} = \underline{\hspace{2cm}}$$

Part c, 10 points

using the method of time constants, find  $a_1$  and  $a_2$  of the circuit transfer function:

$a_1 =$  \_\_\_\_\_

$a_2 =$  \_\_\_\_\_

Part d, 5 points

There may be either 1 or 2 poles of the transfer function.

If the poles are real, give the 1 or 2 pole frequencies in Hz:

$$f_{p1} = \underline{\hspace{2cm}}, \quad f_{p2} = \underline{\hspace{2cm}}$$

If there are 2 poles, and they are complex, give  $f_n = \omega_n / 2\pi$  and the damping factor  $\zeta$  :

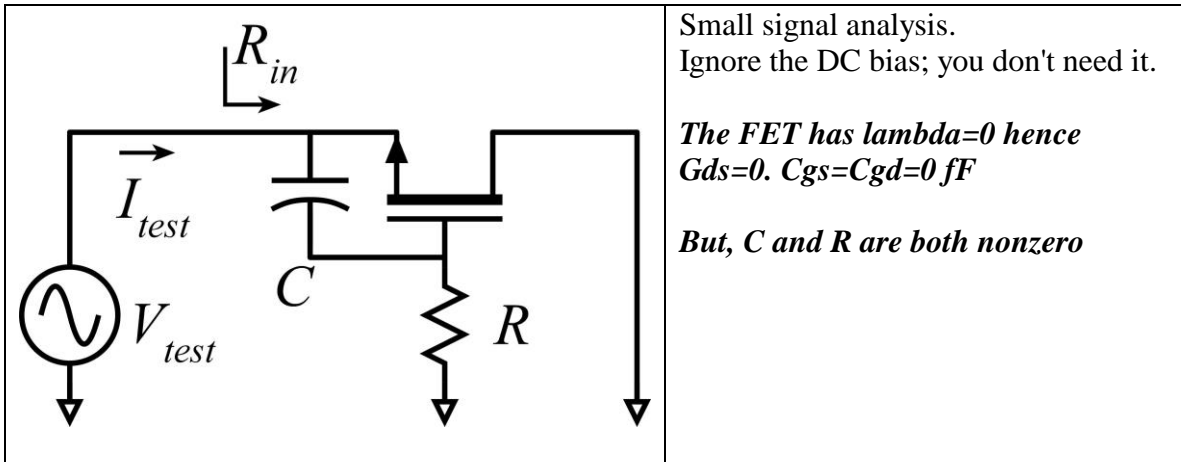
$$f_n = \omega_n / 2\pi = \underline{\hspace{2cm}}, \quad \zeta = \underline{\hspace{2cm}}$$





**Problem 3, 30 points**

Part a 5 points



*Replacing the transistor with its high frequency small-signal model, draw a small-signal equivalent circuit diagram.*

Part b, 10 points

**USING NODAL ANALYSIS**, compute  $Z(s)=V_{\text{test}}(s)/I_{\text{test}}(s)$  in ratio-of-polynomials form:

$$Z(s) = Z_{\text{mid-band}} \times (s\tau)^m \times \frac{1 + b_1s + b_2s^2 + \dots}{1 + a_1s + a_2s^2 + \dots} = \underline{\hspace{10cm}}$$

***here  $m$ , an integer, can be positive or negative or zero***



Part c, 10 points

$$g_m = 1 \text{ mS}, R = 100 \text{ k}\Omega, C = 1 \text{ pF}$$

Find the frequencies of any zeros (there may be zero, one or two present) in  $Z(s)$ :

$$f_{z1} = \text{_____}, f_{z2} = \text{_____}, \dots$$

There may be either 1 or 2 poles in  $Z(s)$ .

If the poles are real, give the 1 or 2 pole frequencies in Hz:

$$f_{p1} = \text{_____}, f_{p2} = \text{_____}$$

If there are 2 poles, and they are complex, give  $f_n = \omega_n / 2\pi$  and the damping factor  $\zeta$  :

$$f_n = \omega_n / 2\pi = \text{_____}, \zeta = \text{_____}$$



Part d, 5 points

Can you describe the behavior of  $Z(s)$  in terms of a simpler equivalent circuit ?